

**II B.Tech II Semester Examinations, APRIL 2011**  
**FORMAL LANGUAGES AND AUTOMATA THEORY**  
**Computer Science And Engineering**

Time: 3 hours

Max Marks: 75

**Answer any FIVE Questions**  
**All Questions carry equal marks**

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1. (a) Construct DFA and NFA accepting the set of all strings not containing 101 as a substring.  
 (b) Draw the transition diagram of a FA which accepts all strings of 1's and 0's in which both the number of 0's and 1's are even.  
 (c) Define NFA with an example. [6+5+4]
  
2. Discuss about
  - (a) Context Free Grammar
  - (b) Left most derivation
  - (c) Right most derivation
  - (d) Derivation tree. [15]
  
3. (a) If  $G = (\{S\}, \{0, 1\}, \{S \rightarrow 0S1, S \rightarrow \varepsilon\}, S)$ , find  $L(G)$ .  
 (b) If  $G = (\{S\}, \{a\}, \{S \rightarrow SS\}, S)$  find the language generated by  $G$ . [7+8]
  
4. (a) What is unrestricted grammar? Give an Example.  
 (b) Explain the language generated by unrestricted grammar.  
 (c) Write about the machine corresponding to unrestricted grammar. [5+5+5]
  
5. (a) Construct a DFA with reduced states equivalent to the regular expression  $10 + (0 + 11)0^* 1$ .  
 (b) Prove  $(a + b)^* = a^*(ba^*)^*$  [7+8]
  
6. (a) Construct a Mealy machine which can output EVEN, ODD according as the total number of 1's encountered is even or odd. The input symbols are 0 and 1.  
 (b) Construct Moore machine equivalent to Mealy machine described in (a). [8+7]
  
7. (a) Convert the following Push Down Automata to Context Free Grammar  
 $M = (\{q_0, q_1\}, \{a, b\}, \{z_0, z_a\}, \delta, q_0, z_0, \varphi)$   
 $\delta$  is given by  
 $\delta(q_0, a, z_0) = (q_0, z_a z_0)$   
 $\delta(q_0, a, z_a) = (q_0, z_a z_a)$   
 $\delta(q_0, b, z_a) = (q_1, \varepsilon)$   
 $\delta(q_1, b, z_a) = (q_1, \varepsilon)$   
 $\delta(q_1, \varepsilon, z_0) = (q_1, \varepsilon)$

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**R09**

**Set No. 2**

- (b) Write the corresponding language for above Push Down Automata. [13+2]
8. Design Turing Machine to increment the value of any binary number by one. The out put should also be a binary number with value one more the number given. [15]

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1. (a) Define NFA with  $\epsilon$  moves.  
 (b) differentiate Moore and Mealy machines.  
 (c) Write the steps in minimization of FA. [4+5+6]
2. (a) Write and explain the properties of transition function.  
 (b) Prove that for any transition function  $\delta$  and for any two input strings  $x$  and  $y$ ,  $\delta(q, xy) = \delta(\delta(q, x), y)$ .  
 (c) Define Finite Automata and Transition diagram. [6+5+4]
3. Describe, in the English language, the sets represented by the following regular expressions:  
 (a)  $a(a+b)^*ab$   
 (b)  $a^*b + b^*a$  [15]
4. (a) What is type1 grammar? Give an Example.  
 (b) Explain the language generated by type1 grammar.  
 (c) Write about the machine corresponding to type1 grammar. [5+5+5]
5. Design Turing Machine for  $L = \{ a^n b^n c^n \mid n \geq 1 \}$ . [15]
6. (a) Let  $G$  be the grammar.  $S \rightarrow aS \mid aSbS \mid \epsilon$ . Prove that  $L(G) = \{x \mid \text{such that each prefix of } x \text{ has atleast as many } a\text{'s as } b\text{'s}\}$   
 (b) Show that  $\{abc, bca, cab\}$  can be generated by a regular grammar whose terminal set is  $\{a, b, c\}$  [8+7]
7. (a) Show that the grammar is ambiguous  
 $S \rightarrow a \mid Sa \mid bSS \mid SSb \mid SbS$ .  
 (b) Find Context Free Grammar for  $L = \{a^i b^j c^k \mid j=i \text{ or } j=k\}$ . [7+8]
8. Which of the following are CFL's? explain  
 (a)  $\{a^i b^j \mid i \neq j \text{ and } i \neq 2j\}$   
 (b)  $\{a^i b^j \mid i \geq 1 \text{ and } j \geq 1\}$   
 (c)  $\{(a+b)^* - \{a^n b^n \mid n \geq 1\}\}$   
 (d)  $\{a^n b^n c^m \mid n \leq m \leq 2n\}$ . [15]

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1. Describe the following sets by regular expressions
  - (a) {101}
  - (b) {abba}
  - (c) {01,10}
  - (d) {a, ab} [15]
2. (a) Draw the transition diagram for a NFA which accepts all strings with either two consecutive 0's or two consecutive 1's.
- (b) differentiate NFA and DFA.
- (c) Construct DFA accepting the set of all strings with atmost one pair of consecutive 0's and atmost one pair of consecutive 1's. [6+4+5]
3. State and explain about closure properties of Context Free Languages. [15]
4. Obtain Chomsky Normal form for following Context Free Grammar  
 $S \rightarrow \sim S \mid [S > S] \mid p \mid q.$  [15]
5. (a) Construct a NFA accepting {ab, ba} and use it to find a deterministic automaton accepting the same set.
- (b)  $M = (\{q_1, q_2, q_3\}, \{0, 1\}, \delta, q_1, \{q_3\})$  is a NFA where  $\delta$  is given by
 
$$\begin{aligned} \delta(q_1, 0) &= \{q_2, q_3\}, & \delta(q_1, 1) &= \{q_1\} \\ \delta(q_2, 0) &= \{q_1, q_2\}, & \delta(q_2, 1) &= \emptyset \\ \delta(q_3, 0) &= \{q_2\}, & \delta(q_3, 1) &= \{q_1, q_2\} \end{aligned}$$
 construct an equivalent DFA. [7+8]
6. (a) Design Turing Machine over {0,1},  $L = \{w \mid |w| \text{ is a multiple of } 3\}$ .
- (b) Draw the transition diagram for above language. [11+4]
7. (a) Find the language generated by the grammar.  $S \rightarrow 0A \mid 1S \mid 0 \mid 1, A \rightarrow 1A \mid 1S \mid 1$
- (b) Construct context-free grammars to generate the set  $\{a^l b^m c^n \mid \text{one of } l, m, n \text{ equals } 1 \text{ and the remaining two are equal}\}$ . [7+8]
8. Construct LR(0) items for the grammar given find it's equivalent DFA.  
 $S' \rightarrow S$   
 $S \rightarrow AS \mid a$   
 $A \rightarrow aA \mid b$  [15]

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**R09**

**Set No. 1**

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1. Find regular expressions representing the following sets
  - (a) the set of all strings over  $\{0, 1\}$  having at most one pair of 0's or at most of one pair of 1's
  - (b) the set of all strings over  $\{a, b\}$  in which the number of occurrences of a is divisible by 3
  - (c) the set of all strings over  $\{a, b\}$  in which there are at least two occurrences of b between any two occurrences of a.
  - (d) the set of all strings over  $\{a, b\}$  with three consecutive b's.

[15]
  
2. (a) What is generating variable? Give example.  
 (b) Reduce the following Context Free Grammar
 
$$\begin{aligned} S &\rightarrow aAa \\ A &\rightarrow sb / bCC / DaA \\ C &\rightarrow abb / DD \\ E &\rightarrow aC \\ D &\rightarrow aDA \end{aligned}$$

[4+11]
  
3. Construct
  - (a) A context-free but not regular grammar.
  - (b) A regular grammar to generate  $\{a^n \mid n \geq 1\}$ .

[15]
  
4. (a) Construct a transition system which can accept strings over the alphabet a, b, .... containing either cat or rat.  
 (b) Show that there exist no finite automaton accepting all palindromes over  $\{a, b\}$ .
 

[7+8]
  
5. Design Push Down Automata for the language  $L = \{wcw^R \mid w \in (0+1)^*\}$ .
 

[15]
  
6. Consider the grammar given below
 
$$\begin{aligned} S &\rightarrow Aa \\ A &\rightarrow AB \mid \varepsilon \\ B &\rightarrow aB \mid b \end{aligned}$$
  - (a) Find the CLOSURE ( $S' \rightarrow .S$ )
  - (b) GOTO( $\{A \rightarrow .AB\}, [B \rightarrow .aB], A$ )

[7+8]

7. (a) Draw the transition diagram and transition table of FA which accept the set of all strings over the alphabet  $\{0, 1\}$  with equal number of 0's and 1's such that each prefix has atmost one more 0 than 1's and atmost one more 1 than 0's.
- (b) Draw transition diagram and transition table of NFA which accepts the set of all strings over an alphabet  $\{0, 1\}$ , beginning with a '1' which, interpreted as the binary representation of an integer is congruent to 0 modulo 5. And construct an equivalent DFA. [6+9]
8. Design Turing Machine to find 2's complement of a given binary number. [15]

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